

State transition models of biomolecular dynamics

A few research questions

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SIMAI 2006, Special Session S2
Baia Samuele (RG), 25/05/2006

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State transition dynamics: basic concepts

- **state transition (ST) dynamics:** (S, q)
 - S : (discrete) **state space**
 - $q : S \rightarrow \mathcal{P}(S)$: [total] transition **dynamics**
 - $x \rightarrow y \stackrel{\text{def}}{=} y \in q(x)$: (binary) transition relation
 - $q(X) \stackrel{\text{def}}{=} \bigcup_{s \in X} q(s)$: extension to **quasistates** $X \subseteq S$
- **orbit** : $(X_i | i \in \mathbb{N})$ t.c. $\forall i. X_{i+1} = q(X_i)$
- **eventually periodic** orbit of origin X :
 $\exists k \geq 0 \exists n > 0. q^{k+n}(X) = q^k(X)$ (**periodic** orbit if $k = 0$)
- orbit (**eventually**) **included** in another one: $(\exists i \geq 0.) \forall j (\geq i) X_j \subseteq X'_j$
- **basin** B : $\emptyset \neq B \subseteq S$ s.t. $q(B) \subseteq B$
- **s-trajectory** : $\xi : \mathbb{N} \rightarrow S$ s.t. $\xi(0) = s$ and $\forall i \geq 0. \xi(i) \rightarrow \xi(i+1)$
- **s-flight** $\stackrel{\text{def}}{=} \text{injective s-trajectory}$

Deterministic ST dynamics: recurrence, attractors

Classical dynamics concepts:

attracting set, recurrence, attractor

- take **two distinct modal flavours** in the general, nondeterministic case, see [(Manca *et al.*, 2005), (Scollo *et al.*, 2006)]
- no modal difference in the **deterministic case** (where the concepts of orbit and trajectory practically coincide):
- state x is **recurrent** if $x \in q^n(x)$ for some $n > 0$
- an **attracting set** A of a basin B is a nonempty subset of B s.t.
 $\forall x \in B \exists k \in \mathbb{N} : \forall n \geq k q^n(x) \subseteq A$
- the **attractor** of a basin B is a minimal attracting set of B (under inclusion)
- the attractor of a basin B exists iff B has no flights
- when the attractor of B exists, it is the set of recurrent states in B

ST dynamics: a contrived example

a simple model of epidemic propagation

as well as of unstable catalytic reaction:



- **instability** of agent **G**: it either dies or recovers (becoming immune: **K**)
- **states** : $(|C| + |K|, |G|)$
- **transitions** can be determined by equipping rules with a measure of **relative strength**

P systems: basic concepts

P systems: a computational model based on

- **multiset rewriting rules**
- workspace **compartmentalization**
- *biological counterparts*:
 - **biochemical reactions**
 - **membranes**
- evolution strategies in (variants of) P systems:
 - **maximal parallelism**, usually
 - or some other **fixed** strategy
- this is **inadequate** to model most biological phenomena: evolution depends on the state, so strategy may **change**

Metabolic P systems

a possible way out: **metabolic** P systems
[(Bianco *et al.*, 2006a), (Bianco *et al.*, 2006b),
(Manca, 2006)]:

- **metabolic rules**: multiset rewriting rules equipped with **reaction maps**:
real-valued functions of the system state, that tell the **competitive strength** of each metabolic rule
- each metabolic rule:
 - **consumes** finite amounts of those biochemical resources whose **types** occur in the **pattern** (the lhs)
 - **produces** corresponding amounts of biochemical resources according to its rhs

P metabolic algorithm

generalizing Avogadro's molar units:

- only finite amounts of biochemical resources are available: their allocation to rules obeys a **mass partition principle**, where each rule gets an amount of each needed resource that is an integer multiple of the rule's **reaction unit**
- the latter depends on the reaction map and on the number of occurrences of resource types in the pattern
- **PMA** [(Manca, 2006)] is the simple algorithm that, at each state, computes the resource allocation to metabolic rules according to their reaction maps and reaction units

Research questions: state transition dynamics

Moving from structureless to topological state spaces:



- definability of **weaker** notions of **recurrence**
that is: replace **exact** occurrence of a state in its own trajectory with **approximate** occurrence
- definability of **weaker** notions of **attraction**
that is: replace **exact** inclusion of orbits in the attracting set with **approximate** inclusion
- **generalization** of the characterization results obtained in [(Scollo *et al.*, 2006)], linking recurrence and attractors, under the aforementioned weakenings
at least for the **deterministic case**

Research questions: metabolic P system models




two levels in metabolic P system modeling of biochemical dynamics:

- **stoichiometry**: the metabolic rules
- **regulation**: the reaction maps
- basic question (roughly): **how to get those models...**
... for a given biochemical behaviour?
This is the general **simulation problem**
- easier (?) question: assume the rules are given, how to get their **reaction maps**?
This may be called the **regulation problem**
- even easier (??) question: assumes the rules are given and the **form** of reaction maps is known (polynomial, say), how to get the values of their **unknown parameters** (the coefficients, say)?
This may be called the **tuning problem**
- an instructive case study:
Goldbeter's model of mitotic oscillation in early amphibian embryos

State transition dynamics

-  V. Manca, G. Franco, G. Scollo
State transition dynamics: basic concepts and molecular computing perspectives.
Chapter 2 in: M. Gheorghe & M. Holcombe (Eds.)
Molecular Computational Models: Unconventional Approaches
Idea Group, Hershey, PA, USA (2005) 32–55.
-  G. Scollo, G. Franco, V. Manca
A relational view of recurrence and attractors in state transition dynamics.
Proc. ReIMiCS/AKA 2006
Manchester, 29 August – 2 September, 2006.
Springer, LNCS (2006) to appear.

Metabolic P systems

-  L. Bianco, F. Fontana, G. Franco, V. Manca
P Systems for Biological Dynamics.
in: G. Ciobanu, M.J. Pérez-Jiménez, G. Paun (Eds.)
Applications of Membrane Computing
Springer, Natural Computing Series (2006) 81–126.
-  L. Bianco, F. Fontana, V. Manca
P Systems with reaction maps.
Int'l J. of Foundations of Computer Science,
vol. 17:1, 2006, 27–48.
-  V. Manca
Topics and Problems in Metabolic P Systems.
Fourth Brainstorming on Membrane Computing
Sevilla, 2006.