

# State transition models of biomolecular dynamics

## A few research questions

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# Overview

- 1 **State transition dynamics**
  - Basic concepts
  - Recurrence and attractors
  - Simple example
- 2 **Metabolic P systems**
  - Basic concepts
  - P metabolic algorithm
- 3 **Research outlook**
  - Research questions: state transition dynamics
  - Research questions: metabolic P system models
- 4 **References**
  - State transition dynamics
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- **state transition (ST) dynamics**:  $(S, q)$

$S$ : (discrete) **state space**

$q: S \rightarrow \mathcal{P}(S)$ : [total] transition **dynamics**

$x \rightarrow y \stackrel{\text{def}}{=} y \in q(x)$ : (binary) transition relation

$q(X) \stackrel{\text{def}}{=} \bigcup_{s \in X} q(s)$ : extension to **quasistates**  $X \subseteq S$

- **orbit**:  $(X_i | i \in \mathbb{N})$  t.c.  $\forall i. X_{i+1} = q(X_i)$

- **eventually periodic** orbit of origin  $X$ :

$\exists k \geq 0 \exists n > 0. q^{k+n}(X) = q^k(X)$  (**periodic** orbit if  $k = 0$ )

- orbit (**eventually**) **included** in another one:  $(\exists i \geq 0.) \forall j (\geq i) X_j \subseteq X'_j$

- **basin**  $B$ :  $\emptyset \neq B \subseteq S$  s.t.  $q(B) \subseteq B$

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- **s-flight**  $\stackrel{\text{def}}{=} \text{injective s-trajectory}$

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# Deterministic ST dynamics: recurrence, attractors

Classical dynamics concepts:

**attracting set, recurrence, attractor**

- take **two distinct modal flavours** in the general, nondeterministic case, see [(Manca *et al.*, 2005), (Scollo *et al.*, 2006)]
- no modal difference in the **deterministic case** (where the concepts of orbit and trajectory practically coincide):
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a simple model of epidemic propagation

as well as of unstable catalytic reaction:



- **instability** of agent **G**: it either dies or recovers (becoming immune: **K**)
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- **transitions** can be determined by equipping rules with a measure of **relative strength**

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- **P systems:** a computational model based on
  - multiset rewriting rules
  - workspace compartmentalization
- *biological counterparts:*
  - biochemical reactions
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  - maximal parallelism, usually
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a possible way out: **metabolic** P systems  
[(Bianco *et al.*, 2006a), (Bianco *et al.*, 2006b),  
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- **metabolic rules**: multiset rewriting rules equipped with **reaction maps**:  
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generalizing Avogadro's molar units:

- only finite amounts of biochemical resources are available: their allocation to rules obeys a **mass partition principle**, where each rule gets an amount of each needed resource that is an integer multiple of the rule's **reaction unit**
- the latter depends on the reaction map and on the number of occurrences of resource types in the pattern
- **PMA** [(Manca, 2006)] is the simple algorithm that, at each state, computes the resource allocation to metabolic rules according to their reaction maps and reaction units

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# Research questions: state transition dynamics

Moving from structureless to topological state spaces:

- definability of **weaker** notions of **recurrence**

that is: replace **exact** occurrence of a state in its own trajectory  
with **approximate** occurrence

- definability of **weaker** notions of **attraction**

that is: replace **exact** inclusion of orbits in the attracting set  
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- **generalization** of the characterization results obtained in  
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**two levels** in metabolic P system modeling of biochemical dynamics:

- **stoichiometry**: the metabolic rules
- **regulation**: the reaction maps
- basic question (roughly): **how to get those models...**
  - ... for a given biochemical behaviour?
  - This is the general **simulation problem**
- easier (?) question: assume the rules are given, how to get their **reaction maps?**
  - This may be called the **regulation problem**
- even easier (??) question: assumes the rules are given and the **form** of reaction maps is known (polynomial, say), how to get the values of their **unknown parameters** (the coefficients, say)?
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State transition dynamics: basic concepts and molecular computing perspectives.

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