## Controlling a Rotating Arm

#### Corrado Santoro

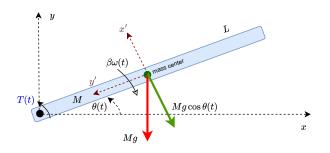
#### ARSLAB - Autonomous and Robotic Systems Laboratory

Dipartimento di Matematica e Informatica - Università di Catania, Italy



Robotic Systems

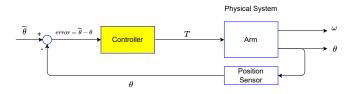
## The Arm



### Discretisation

$$\omega(k+1) = (1 - \frac{3}{2} \frac{\Delta T}{ML} \beta) \omega(k) - \frac{3}{2} \frac{\Delta T}{L} g \cos \theta(k) + \frac{3\Delta T}{ML^2} T(k)$$

$$\theta(k+1) = \theta(k) + \omega(k) \Delta T$$

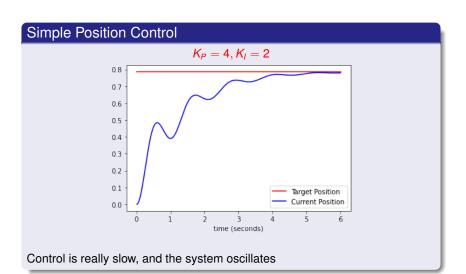


### Simple Position Control

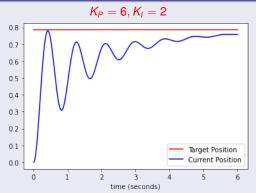
- Let us a consider a "simple" position controller
- For the cart a P Controller has been enough, but...
- in the arm, the presence of gravity requires a "push" (non-zero output) in case of error = 0
- A PI Controller is mandatory
- However, the natural oscillating behaviour of the system creates some hard problems...

(see examples/simple\_control/arm\_simple\_position\_control\_PID.ipynb)



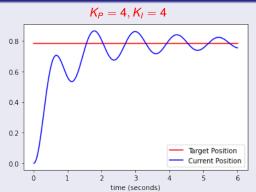






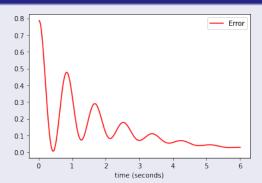
Incrementing  $K_P$  does not help...

## Simple Position Control



Also incrementing  $K_l$  does not help...

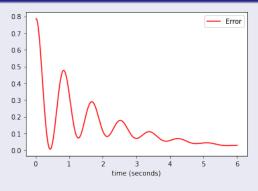
### Let's Analyse the trend of the error



- When the error decreases, the control action is OK
- When the error increases, we need more control action



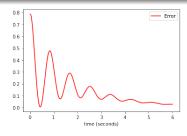
### Let's derivate the error



$$\dot{e} = \frac{de(t)}{dt}$$

- When the error decreases,  $\dot{e} < 0$ , the control action is OK
- When the error **increases**,  $\dot{e} > 0$ , we can increase control action





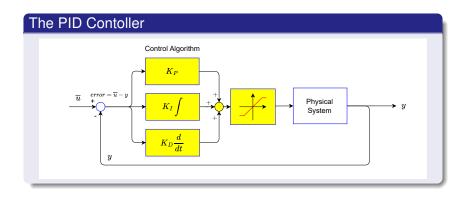
#### The PID Controller

Let's add a factor proportional to the derivative of the error:

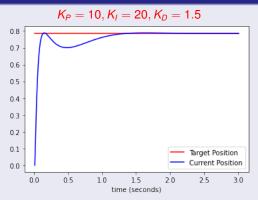
$$ControlAction = PI(error) + K_D \dot{e}$$

- When the error **decreases**,  $\dot{e} < 0$ , so the derivative action acts a as "brake" reducing the control action (this is OK, because the trend of the error is, in any case, decreasing)
- When the error increases,  $\dot{e} > 0$ , so the derivative factor improves the control action





#### The PID Contoller



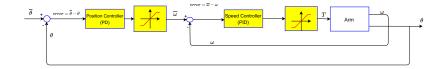
(see examples/simple\_control/arm\_simple\_position\_control\_PID.ipynb)

- System is fast and no oscillation occurs
- The value of  $K_l$  (that is high) is needed due the fact that we must compensate the gravity



# Position and Speed Control

Position and Speed Cascading Control

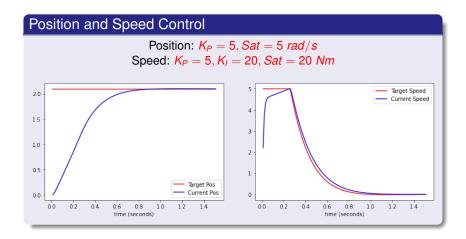


### Position and Speed Control

- As in the cart, also in the arm the best solution for position control is the double loop position + speed
- In oscillating systems, the position controller is usually a PD, while the speed controller is usually a PID

(see examples/position\_control/arm\_position\_control.ipynb and godot/arm\_no\_physics/)





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