

CTF-DCT approach

- Let **I** be a digital image.
- Following the **JPEG pipeline**, **I** is divided into non-overlapping blocks of size **8x8**.
- The **Discrete Cosine Transform (DCT)** is then applied to each block, formally:

$$F[u, v] = \frac{1}{4} C(u)C(v) \left[\sum_{x=0}^7 \sum_{y=0}^7 I[x, y] \cos(a) \cos(b) \right]$$

where

$$a = \frac{(2x + 1)u\pi}{16}, b = \frac{(2y + 1)v\pi}{16}, C(u) = \begin{cases} \frac{1}{\sqrt{2}} & u = 0 \\ 1 & u > 0 \end{cases}, C(v) = \begin{cases} \frac{1}{\sqrt{2}} & v = 0 \\ 1 & v > 0 \end{cases}$$

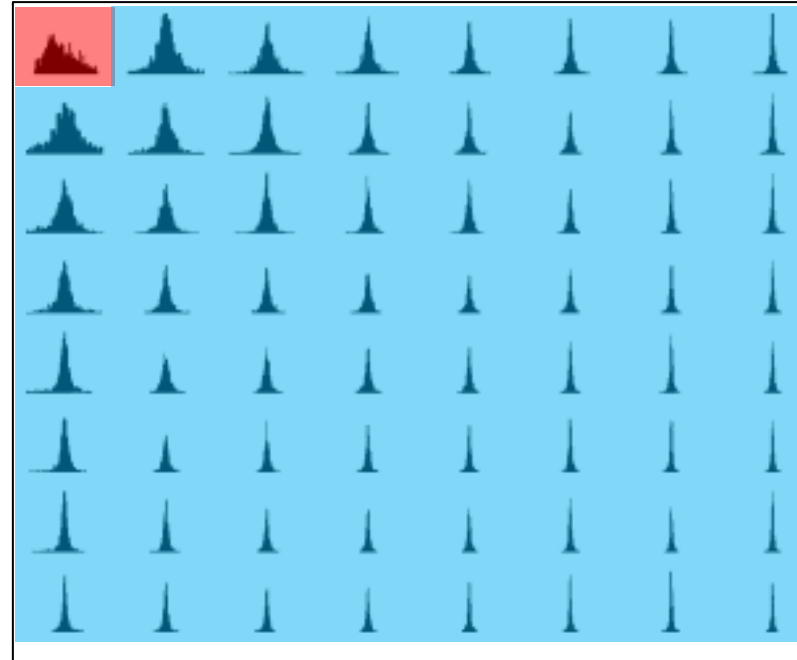
DCT

DC coefficient

DC coefficient

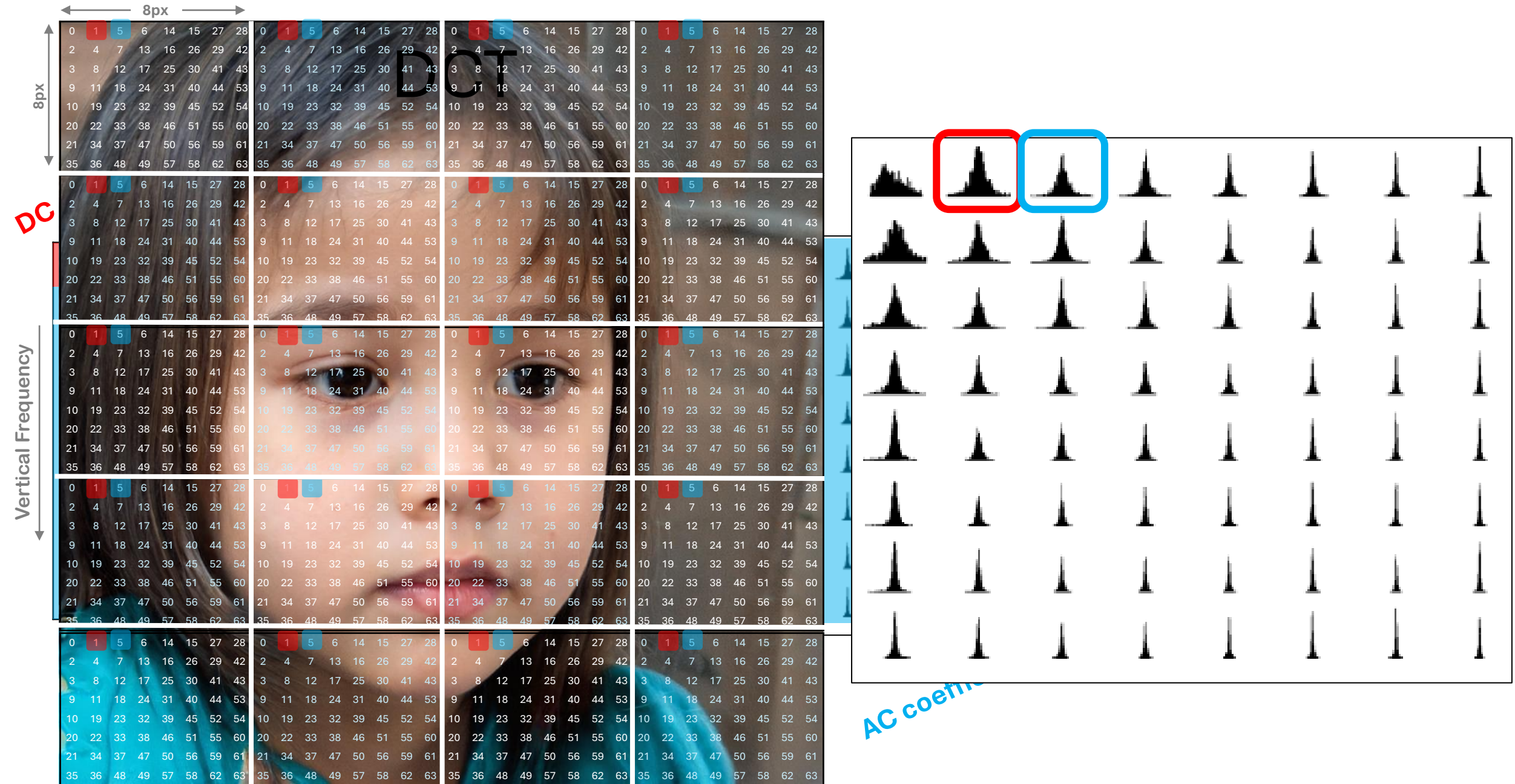
Vertical Frequency
↓

0	1	5	6	14	15	27	28
2	4	7	13	16	26	29	42
3	8	12	17	25	30	41	43
9	11	18	24	31	40	44	53
10	19	23	32	39	45	52	54
20	22	33	38	46	51	55	60
21	34	37	47	50	56	59	61
35	36	48	49	57	58	62	63



AC coefficients

AC coefficients



DCT

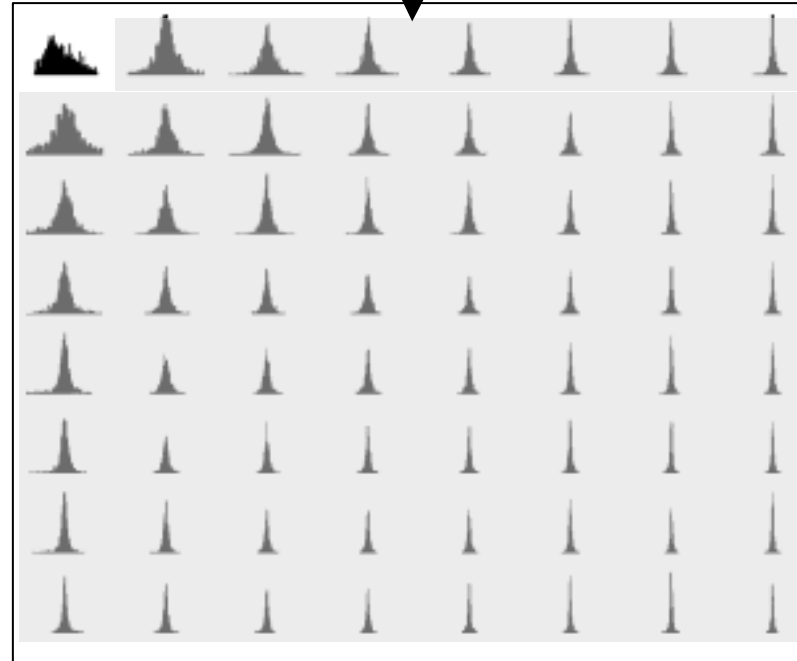
DC coefficient

Horizontal Frequency

Vertical Frequency

0	1	5	6	14	15	27	28
2	4	7	13	16	26	29	42
3	8	12	17	25	30	41	43
9	11	18	24	31	40	44	53
10	19	23	32	39	45	52	54
20	22	33	38	46	51	55	60
21	34	37	47	50	56	59	61
35	36	48	49	57	58	62	63

AC coefficients



Lam, Edmund Y., and Joseph W. Goodman. "A mathematical analysis of the DCT coefficient distributions for images." *IEEE transactions on image processing* 9.10 (2000): 1661-1666.

Laplacian distribution

$$P(x) = \frac{1}{2\beta} \exp\left(\frac{-|x - \mu|}{\beta}\right)$$

$$\beta = \frac{\sigma}{\sqrt{2}}$$

