Immune Algorithms with Aging Operators for the String Folding Problem and the Protein Folding Problem

V. Cutello, G. Morelli, G. Nicosia, and M. Pavone

Department of Mathematics and Computer Science, University of Catania, V.le A. Doria 6, 95125 Catania, Italy {cutello, morelli, nicosia, mpavone}@dmi.unict.it

Abstract. We present an Immune Algorithm (IA) based on clonal selection principle and which uses memory B cells, to face the protein structure prediction problem (PSP) a particular example of the String Folding Problem in 2D and 3D lattice. Memory B cells with a longer life span are used to partition the funnel landscape of PSP, so to properly explore the search space. The designed IA shows its ability to tackle standard benchmarks instances substantially better than other IA's. In particular, for the 3D HP model the IA allowed us to find energy minima not found by other evolutionary algorithms described in literature.

Keywords: Clonal selection algorithms, aging operator, memory B cells, protein structure prediction, HP model, functional model proteins.

1 The String and Protein Folding Problems

A d-dimensional lattice is a graph $\mathcal{L} = (V, E)$, where $V \subseteq \mathbb{Z}^d$, i.e. the vertices are points in the Euclidean space with integer coordinates, and the set of edges $E \subseteq \{(x,y) : x = (x_1,\ldots,x_d), y = (y_1,\ldots,y_d)\}: \sum_{i=1}^d |x_i-y_i| = 1\}.$ Let now $s = \langle s_1, \dots, s_i, \dots, s_n \rangle$ be a string of length n in the alphabet $\{0, 1\}^*$. By folding of the string s we mean its embedding into the lattice \mathcal{L} , i.e., a one-to-one mapping f from the set $\{1 \leq j \leq n\}$ to V such that for all $1 \leq j \leq n-1$ we have $(f(j), f(j+1)) \in E$. The points f(j) and f(j+1) are called f – neighbors. A folding can therefore be seen as a walk in the lattice. A folding of a string s is a self-avoiding walk iff two characters s_i, s_j with $i \neq j$ do not occupy the same node of the lattice. Given a folding f of a string s, we can also introduce a measure to "assess" the quality of f. We say that an edge $(x,y) \in L$ is a loss if the two vertices are not f - neighbors, and exactly one of them is the image under f of a symbol $s_i = 1$ Given a d-dimensional lattice $\mathcal{L} = (V, E)$, a string $s \in \{0,1\}^*$, and an integer k, the STRING FOLDING PROBLEM (SFP) is be defined as the problem of checking whether there exists a self-avoiding folding of s into the lattice \mathcal{L} , with k or fewer losses. Let now d=2, and let $L = \{p = (x_p, y_p) : 0 \le x_p, y_p \le n - 1\}$. The neighborhood of a point p is defined

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as the set of points in the lattice L connected by a single edge to p, i.e. as the set $\mathcal{N}(p) = \{q \in L : |x_p - x_q| + |y_p - y_q| = 1\}$. One of the main characteristics of a lattice "geometry" is the number of nodes directly connected to each node. Such a number is usually the same for all nodes, and it is known as the *coordination number* (C_n) of the lattice. For instance, in two dimensions we have honeycomb lattice $(C_n = 3)$, square lattice $(C_n = 4)$, and triangular lattice $(C_n = 6)$. In three dimensions possible lattice geometries are the following: diamond lattice $(C_n = 4)$, cubic lattice $(C_n = 6)$, and tetrahedral lattice $(C_n = 12)$.

1.1 The Protein Folding Problem

The special case of the STRING FOLDING PROBLEM with d=2, and square lattice $(C_n=4)$, captures the protein folding problem in the 2D HP model [6]. Analogously for d=3 and cubic lattice $(C_n=6)$ we have the 3D HP model [6]. The HP model was shown to be NP complete problem for 2D lattice [12] (the NP-hardness is shown by reduction from an interesting variation of the planar Hamilton cycle problem), and for 3D lattice [13] (the NP-hardness is shown by reduction from a variation of the Bin Packing problem).

The HP model is a well-known approach to face the protein folding problem. It models proteins as 2D or 3D self-avoiding walks (i.e. two residues cannot occupy the same side of the lattice) of ℓ monomers on the square lattice. There are only two monomer types: the H and the P monomers, respectively for hydrophobic and polar monomers. Then, the HP model reduces the alphabet from 20 characters to 2, where our protein sequences take the form of strings belonging to the alphabet $\{H, P\}^+$. Any feasible conformation in the HP model is assigned a free energy level: each H-H topological contact, that is, each lattice nearestneighbor H-H contact interaction, has energy value $\epsilon \leq 0$, while all other contact interaction types (H-P, P-P) contribute with $\delta \geq 0$ value to the total free energy. In general, in the HP model the residues interactions can be defined as follows: $e_{HH} = \epsilon$ and $e_{HP} = e_{PH} = e_{PP} = \delta$. When $\epsilon = -1$ and $\delta = 0$ we have the typical interaction energy matrix for the standard HP model [6], whereas when $\epsilon = -2$ and $\delta = 1$ we have the energy matrix for the shifted HP model [7, 17]. The native state of a protein is a conformation that minimizes the free energy function and, hence, the conformation that maximizes the number of contacts H–H.

In this paper we will present experimental results on the PFP, i.e. the SFP using square lattice $(C_n = 4)$, and cubic lattice $C_n = 6$. In particular, we design and test an Immune Algorithm (IA) using classical PFP instances of the *Tortilla 2D HP Benchmarks*¹, 3D cubic lattice HP instances (taken from [8,9]), and the classical benchmarks for the Functional Model Proteins², into 2D square lattice. The 3D HP benchmark uses the same protein sequences of Tortilla 2D HP Benchmarks using a 3D cubic lattice. We also note that each instance of the functional model proteins benchmarks has a unique native fold with minimal energy value, E^* , and an energy gap between E^* and the first excited state (best suboptimal).

¹ http://www.cs.sandia.gov/tech_reports/compbio/tortilla-hp-benchmarks.html

² http://www.cs.nott.ac.uk/~nxk/HP-PDB/2dfmp.html

Finally we note that in the HP model, a protein is represented as a sequence in a lattice in either two or three dimensions. The sequence is the set of coordinates that give the position in the lattice of each ammino-acid of the protein. Given the position in a lattice for the first ammino-acid of the protein, the sequence can be also identified by a set of moves that allow to find the position in the lattice of an ammino-acid using the position of the previous one. In this scenario the folding is represented by a sequence of moves (directions) that allow to find a sequence with the maximum number of topological contact.

2 The Clonal Selection Algorithm for the PFP

In this article we describe an improved version of a previously proposed immune algorithm [14], that uses only two entity types: antigens (Ag) and B cells. The Ag is the given input string $s \in \{0,1\}^*$ of the SFP and it models the hydrophobicpattern of the given protein, that is a sequence $s \in \{H, P\}^{\ell}$, where ℓ is the protein length. The B cells population, $P^{(t)}$ (of size k), represents a set of candidate solution in the current fitness landscape at each generation t. The B cell, or B cell receptor, for the 2D HP model is a sequence of directions $r \in \{F, L, R\}^{\ell-1}$, with F = Forward, L = Left, and R = Right, where each r_i , with $i = 2, ..., \ell-1$, is a relative direction [11] with respect to the previous direction r_{i-1} (i.e., there are ℓ -2 relative directions) and r_1 is the non-relative direction. Analogously, for the 3D HP model, the B cell receptor is a sequence $r \in \{F, L, R, B, U, D\}^{\ell-1}$, where B = 0Backward, U = Up, and D = Down. The sequence r detects a conformation suitable to compute the energy value of the hydrophobic-pattern of the given protein. For the 2D protein instances we use the relative directions because their performance are better with respect to absolute directions in the square lattice [11], while for the 3D protein instances we use both coding: relative and absolute directions to assess the effectiveness of the IA. The initial population, at time t=0, is randomly generated in such a way that each B cell in $P^{(0)}$, represents selfavoiding conformations. The function $Evaluate(P^{(t)})$ computes the fitness value F of each B cell $x \in P^{(t)}$. Then, F(x) = e is the energy of conformation coded in the B cell receptor x, with -e being the number of topological contacts H-Hin the lattice (2D or 3D). The function Termination_Condition() returns true if a solution is found, or a maximum number of fitness function evaluations (T_{max}) is reached. The cloning operator, simply, clones each B cell dup times, producing an intermediate population P^{clo} of size $Nc = k \times dup$. We tested our IA using the combination of inversely proportional hypermutation and hypermacromutation operators. In the Inversely Proportional Hypermutation operator the number of mutations is inversely proportional to the fitness value. In particular, at each generation t, the operator will perform at most the following mutations:

$$M_i(F(\boldsymbol{x})) = \begin{cases} ((1 - \frac{E^*}{-1}) \times \beta) + \beta, & \text{if } F(\boldsymbol{x}) = 0\\ ((1 - \frac{E^*}{F(\boldsymbol{x})}) \times \beta), & \text{if } F(\boldsymbol{x}) > 0 \end{cases}$$
(1)

with $\beta = c \times \ell$. In this case, $M_i(F(\mathbf{x}))$ has the shape of an hyperbola branch. In the Hypermacromutation operator the number of mutations is determined

by a simple random process. It tries to mutate each B cell receptor M times, maintaining the self-avoiding property. The number of mutations M is at most $M_m(x) = j - i + 1$, in the range [i, j], with i and j being two random integers such that $(i + 1) \leq j \leq \ell$. The number of mutations is independent from the fitness function F and any other parameter. The hypermacromutation operator, for each B cell receptor, randomly selects a perturbation direction, either from left to right (k = i, ..., j) or from right to left (k = j, ..., i).

Table 1. Pseudo-code of the Immune Algorithm for the PFP

```
Immune Algorithm(\ell, k, dup, \tau_B, c)
t := 0; Nc := k * dup;
P^{(t)} := \text{Initial\_Pop}();
\text{Evaluate}(P^{(t)});
\text{while } (\neg \text{Termination\_Condition}()) \text{ do}
P^{(clo)} := \text{Cloning } (P^{(t)}, Nc);
P^{(hyp)} := \text{Hypermutation } (P^{(clo)}, c, \ell);
\text{Evaluate}(P^{(hyp)});
P^{(macro)} := \text{Hypermacromutation } (P^{clo});
\text{Evaluate } (P^{(macro)});
(P_a^{(t)}, P_a^{(hyp)}, P_a^{(macro)}) := \text{Aging}(P^{(t)}, P^{(hyp)}, P^{(macro)}, \tau_B);
P^{(t+1)} := (\mu + \lambda) \text{-Selection } (P_a^{(t)}, P_a^{(hyp)}, P_a^{(macro)});
t := t + 1;
\text{end\_while}
```

In the hypermutation phase, we use the stop at the First Constructive Mutation (FCM) strategy: if a constructive mutation occurs, the mutation procedure will move on to the next B cell. We adopted such a mechanism to slow down (premature) convergence, exploring more accurately the search space. Formally, the mutation operator acts on the population $P^{(clo)}$, where each B cell is a feasible candidate solution, i.e. it is a self-avoiding walk, generating the new populations $P^{(hyp)}$ and $P^{(macro)}$. In 2D lattice, given a protein conformation sequence R, the mutation operator randomly selects a direction r_j , with $1 \le j \le \ell - 1$, or a subsequence $R_{ij} = \langle r_i, r_{i+1}, \ldots, r_{j-1}, r_j \rangle$, with i > 1 and $j \le \ell - 1$. For each relative direction $D = r_j$, a new direction $D' \ne D \in \{F, L, R\}$ is randomly selected. If the new conformation is again self-avoiding then the operator accepts it, otherwise the procedure repeats the process with a new and last direction $D'' \ne \langle D, D' \rangle > \langle F, L, R \rangle$.

Aging. The aging process reflects the attempt to benefit from modelling the limited life spans of B cells and longer life spans of Memory B cells. Starting from this basic observation, the aging operator eliminates old B cells from the populations $P^{(t)}$, $P^{(hyp)}$ and $P^{(macro)}$, so to avoid premature convergence. The parameter τ_B (and τ_{B_m} for the memory B cells) sets the maximum number of

generations allowed to B cells to remain in the population. When a B cell is $\tau_B + 1$ old (or $\tau_{B_m} + 1$ old) it is erased from the current population, no matter what its fitness value is. We call this strategy, static pure aging. During the cloning expansion, a cloned B cell takes the age of its parent. After the hypermutation phase, a cloned B cell which successfully mutates, i.e. with a better fitness value, will be considered to have age equal to 0. Thus, an equal opportunity is given to each "new genotype" to effectively explore the fitness landscape. We note that for τ_B greater than the maximum number of allowed generations, the IA works essentially without aging operator. In such a limit case the algorithm uses a strong elitist selection strategy. Aging is a new operator that causes a turnover in the populations of the IA. Its goal is to generate diversity and to avoid getting trapped into local minima. It is an operator inspired by the biological immune system where there is an expected mean life for the B cell [15], and it is, in general, problem- and algorithm-independent. After clonal expansion and aging phase, a new population $P^{(t+1)}$, of k B cells, for the next generation t+1, is obtained by selecting the best B cells which "survived" the aging operator, from the populations $P^{(t)}$, $P^{(hyp)}$ and $P^{(macro)}$. No redundancy is allowed: each B cell receptor is unique, i.e. each genotype is different from all other genotypes. If only k' < k B cells survived, new randomly created B cells (with aqe = 0) are added by the *Elitist_Merge* function into the population (the *Birth phase*). In general, the selection operator chooses the k best elements from both parent and offspring B cells sets, thus guaranteeing monotonicity in the evolution dynamic. In table 1 we show the pseudo-code of the proposed Immune Algorithm.

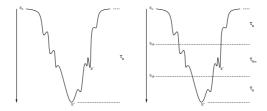


Fig. 1. Typical funnel landscape for the PSP problem (left plot); partitioning of the funnel landscape in three region using memory B cells with two aging parameter values, τ_{B} , and τ_{Bm}

2.1 Partitioning the Funnel Landscape Using Memory B Cells

The proposed IA uses memory B cells to better handle the space of solutions and improve the performance, for the protein structure prediction problem. We have not tested its performance on general instances of the String Folding Problem. One characteristic feature of the PSP problem is its rugged funnel landscape (see fig.1 on the left), where the number of feasible conformations decreases with low free energy values, i.e. many conformations have high energy and few have low energy. Thus, very likely, we could get trapped in a local minimum.

Starting from this simple topological observation we used memory B cells to partition the funnel landscape into three regions. Each partition is obtained using two threshold energy values: if the protein native fold has energy value E^* we have $E_{level} = -E^* + 1$ energy levels, thus the boundary of the first partition and secondary partition are respectively $E_{FP} = -(E_{level} \times 0.67)$ and $E_{SP} = -(E_{level} \times 0.85)$. Theoretical findings [3] and experimental results (not reported in this paper), show that the hardest region to search is the middle one. It is typically rugged with many local minima. So we apply memory B cells only to such a region. Conformations whose energy value is in the middle region, are allowed to maturate.

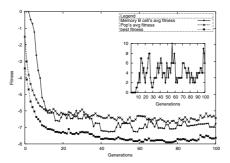


Fig. 2. The best fitness value, average fitness function values of memory B cells and $P^{(t)}$ versus generations on protein sequence Seq2, with parameter $d=10, dup=2, \tau_B=5$ and $\tau_{B_m}=10$. In the inset plot we report the number of memory B cells versus generations

In figure 2 we show memory B cells dynamic. We set the minimal population size value d=10, with dup=2, $\tau_B=5$ and $\tau_{B_m}=10$. All curves are averaged on 30 independent runs. We plot the best fitness value, the average fitness of $P^{(t)}$ and memory B cell populations, whereas in the inset plot we show as change the number of memory B cells with respect to generations.

3 Experimental Results

To assess the overall performance of the new version of the IA using memory B cells we tested it using the well-known tortilla benchmarks in the standard 2D and 3D HP model and the classical protein instances for the Functional Model Proteins.

3.1 HP Model in 2D Square Lattice

In table 2 we compare our improved IA with the previous versions, respectively IA with Hypermacromutation Operator only (with and without elitism) [4], and IA with Inversely Proportional Hypermutation and Hypermacromutation

		Macro w	rith Elit.	Macro wit	hout Elit.	Inv.Prop	.+Macro	IA witl	n mem.
No.	ℓE^*	SR	AES	SR	AES	SR	AES	SR	AES
1	20 -9	96.67	20508.9	100	25418.8	100	14443.7	100	15439.6
2	24 -9	100	37659.7	100	39410.9	100	39644.1	100	46034.9
3	25 - 8	96.67	58905.3	100	79592.1	100	95147	100	99865.7
4	36 - 14	36.67	310291.4	16.67	466176.4	23,33	388323,4	100	2032504
5	48 -23	3.33	277454	6.67	483651.5	(b.f22)	//	56.67	2403985.3
6	50 - 21	53.33	459868	16.67	469941.2	53.33	538936.4	100	1011377.4
7	60 -36	(b.f35)	//	(b.f34)	//	(b.f34)	//	(b.f35)	//
8	64 - 42	(b.f39)	//	(b.f36)	//	(b.f39)	//	(b.f39)	//
9	20 -10	96.67	27719.14	100	27852.1	100	17293.9	100	20135.4

Table 2. IA with memory B cells compared to other types of IA. Results averaged on 30 independent runs

operators [14]. Comparisons were done in terms of Success Rate (SR) and Average number of Evaluations to Solution (AES). The IA used standard parameter values: k = 10, dup = 2, c = 0.4, as described in [14] while the standard B cells have aging parameter $\tau_B = 5$ and the memory B cells $\tau_{B_m} = 10$.

Table 2 shows that the improved IA is comparable on the simplest protein instances to the previous IA versions, and outperforms them on the hard instances. Indeed, the new IA obtained SR=100 on the Seq4 and Seq6, and SR=56.67 on the Seq5, where the other versions failed. For the hardest instances the new IA obtained the lowest energy values. These results show that partitioning the landscape in three groups, is an effective approach for the PSP in the standard 2D HP model.

3.2 HP Model in 3D Cubic Lattice

In the 3D cubic lattice, each point has 6 different neighbors and 5 available locations. We use two different schemes of moves (absolute and relative directions) to represent and embed a protein in the lattice. The relative encoding has been described in section 2: the residues direction are relative to direction of the previous move, while in the absolute directions encoding the residues direction are relative to the axes defined by the lattice. Both for the absolute and relative coding not all moves give a feasible conformation. In our work we force the selfavoidance constraint so each set of moves will correspond to a feasible sequence (feasible conformation). Concerning the experimental results, for all considered instances the IA (working with feasible solutions) has found the known minimum value and for all instances the found mean value is lower than the results obtained in [9] using Evolutionary Algorithms (EAs) working on Feasible-Space. For several sequence presented in [9], as shown in table 3, we have found new best lowest energy values for 3D protein sequences 5, 7, and 8. The IA used the standard parameter values: k = 10, dup = 2, c = 0.4, as described in [14], B cells have aging parameter $\tau_B = 5$ and the memory B cells $\tau_{B_m} = 10$. For the experimental protocol we adopt the same values used in [9]: 50 independent runs and a maximum number of evaluations equal to 10^5 . In [9] the author does not use the SR and AES values as quality metrics, but the following parameters: Best found solution (Best), mean and standard deviation (σ). We designed an

		Absolute Encoding						Relative Encoding					
			F-EA		IA		F-EA			IA			
Seq.	ℓ	Best	Mean	σ	Best	Mean	σ	Best	Mean	σ	Best	Mean	σ
1	20	-11	-10.32	0.61	-11	-11	0	-11	-9.84	0.86	-11	-10.90	0.32
2	24	-13	-10.90	0.98	-13	-13	0	-11	-10.00	0.87	-13	-12.22	0.65
3	25	-9	-7.98	0.71	-9	-9	0	-9	-8.64	0.69	-9	-8.88	0.48
4	36	-18	-14.38	1.26	-18	-16.76	1.02	-18	-13.72	1.41	-18	-16.08	1.02
5	48	-25	-20.80	1.61	-29	-25.16	0.45	-28	-18.90	2.08	-28	-24.82	0.71
6	50	-23	-20.20	1.50	-23	-22.60	0.40	-22	-19.06	1.46	-23	-22.08	1.43
7	60	-39	-34.18	2.31	-41	-39.28	0.24	-38	-32.28	3.09	-41	-39.02	0.50
8	64	-39	-33.01	2.49	-42	-39.08	0.95	-36	-30.84	2.55	-42	-39.07	1.20

Table 3. Results of the IA for the 3D HP model

IA which uses a Penalty strategy and a Repair-based approach as reported in [9] which obtained similar experimental results to [9] (not shown due to space limitation). The used penalty strategy is based on the fact that not all moves of a conformation maintain the self-avoiding property; when a move does not satisfy the self-avoiding constraint, the energy value assigned to the conformation is increased of a penalty coefficient and, also, the aminoacid involved in a collision will be not considered in H-H contact. The repair strategy is applied, after the HyperMutation and HyperMacroMutation phases, on each conformation of the populations that contains a collision, and starting the process from the last collision found. Let i be the collision position, the repair process determines a free position L in the lattice such that it is possible to reach the position i+1with only one move. Moreover, either L is reachable directly from the position i-1 (in this case i will move to position L) or there exists another free position C, reachable from i-2 with only one move, and from which is possible to reach L, with one move (in this case i will move to position L and i-1 to position C). In both cases, the moves of the conformation will be modified according to the new coordinates. Such an IA proved to be very efficient for both absolute and relative encoding, and allowed us to find energy minima not found by other EAs working in feasible spaces and described in literature [9].

3.3 Functional Model Proteins in 2D Square Lattice

We show here the experimental results on the classical benchmarks for the Functional Model Proteins using memory B cells. In table 4 we report the experimental results obtained by our IA using different life span values for the memory B cells: $(\tau_B = 3, \tau_{B_m} = 5)$, $(\tau_B = 4, \tau_{B_m} = 8)$, and $(\tau_B = 5, \tau_{B_m} = 10)$. In the last two columns we report the performance of an IA without memory B cells using the standard parameter values: $k = 10, dup = 2, c = 0.4, \tau_B = 5$. All the experimental results reported are averaged on 30 independent runs. Like in the standard HP Model, the proposed IA obtained the best results using the pair $(\tau_B = 5, \tau_{B_m} = 10)$ values. However, for the functional model proteins the IA without memory B cells outperforms the IA with memory B cells in term of SR and AES, obtaining SR = 100 values on all functional model protein instances, except for the SeqC, where the algorithm reaches SR = 56.67 with mean = -15.13, and

		$\tau_B =$	$3, \tau_{B_m} = 5$	$ \tau_B =$	$4, \tau_{B_m} = 8$	$\tau_B =$	$5, \tau_{B_m} = 10$	τ	$_{B} = 5$
No.	E^*	SR	AES	SR	AES	SR	AES	SR	AES
A	-20	100	253393	100	60664.8	100	38586.63	100	32847.7
В	-17	100	41189.7	100	258387	100	28434.9	100	17526.7
$^{\rm C}$	-16	16.67	31311300	36.67	2448820	43.33	2583300.8	56.67	2667430
D	-20	100	568485	100	261439.1	100	130849	100	128015.1
\mathbf{E}	-17	100	16726.3	100	17586.13	100	20834.46	100	12095.3
F	-13	96.67	1083238.6	100	711828.33	100	483126.76	100	332938.5
G	-26	100	1171346.4	100	936008.9	100	588057.5	100	584179.8
Η	-16	100	107131	100	54432.7	100	42562.53	100	38262.6
I	-15	100	506368	100	75273.8	93.33	907962.4	100	281720.8
J	-14	100	226564.87	100	141515.23	100	100085.43	100	104155.4
K	-15	100	43327.2	100	82361 1	100	71903.1	100	27743 7

Table 4. Improved IA performances using memory B cells (τ_B, τ_{B_m}) in the Functional Model Proteins. Each protein instance has $\ell = 23$ monomers

 $\sigma=0.65$. This confirm the optimal searching ability and diversity generation of the pure aging operator. Finally, in table 5 we show the number of energy evaluations required by the best run (in [10] the authors use only this metric to assess the effectiveness of their algorithm) to reach the optimum or a sub-optimum energy value. We compare the performances of the IA with and without memory B cells with the state of art algorithm for the functional model proteins, the Multimeme Algorithm [10]. Comparing the results both versions of the IA, with or without memory B cells outperforms the Multimeme Algorithm on all the protein instances, in particular the IA without memory B cells obtains the best results (9 instances over 11).

Table 5. Comparison of best runs for MultiMeme Algorithm (MMA) [10] and IA, with and without memory B cells for the Functional Model Proteins. Each protein instance has $\ell=23$ monomers

No.	E^*	MMA	IA without memory B cells	IA with memory B cells
1	-20	15170	3372	3643
2	-17	61940	578	1488
3	-16	132898	319007	100234
4	-20	66774	4955	20372
5	-17	53600	1047	1956
6	-13	32619	2828	7482
7	-26	114930	10061	37841
8	-16	28425	1818	1937
9	-15	25545	3845	10399
10	-14	111046	2847	3462
11	-15	52005	3176	1007

4 Conclusions

In this paper we propose an improved version of an IA for the protein structure prediction problem, in the standard 2D and 3D HP model and the Functional Model Proteins. In [4,14] the results obtained for the 2D HP model suggested that the previous IA version was comparable to and, in many protein instances,

outperformed folding algorithms which are present in literature. The results obtained in this research work established the new IA for the 2D HP model as the state-of-art algorithm for this discrete lattice model. Moreover, for the 3D HP model the IA allowed us to find energy minima not found by other EAs described in literature. Finally, for the functional model protein, the IA, with or without memory B cells, outperforms the Multimeme Algorithm on all the protein instances. Our algorithm proved to be very effective and very competitive, compared to the existing state-of-art EAs.

We intend to analyze now the impact, on the efficiency and efficacy of the Immune Algorithm, of the parameters τ_B and τ_{B_m} . We also believe that it could be worthwhile to implement a mutation rate dependent upon the B cells age.

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