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ADDENDUM TO "REMARKS ON WEAK COMPACTNESS OF OPERATORS DEFINED ON CERTAIN INJECTIVE TENSOR PRODUCTS"

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The idea (used in [1]) of embedding $X \otimes_\varepsilon Y$ into $X^{**} \otimes_\varepsilon Y$, when X is an $\mathscr{L}_\infty$ space can also be used to get the following results.

Theorem 1. *Let X be an $\mathscr{L}_\infty$ space and Y a Banach space. Then $X \otimes_\varepsilon Y$ contains a complemented copy of l^1 iff Y does the same.*

Proof. If l^1 embeds complementably into $X \otimes_\varepsilon Y$, then c_0 embeds into $(X \otimes_\varepsilon Y)^*$, a closed subspace of $(X^{**} \otimes_\varepsilon Y)^*$; then l^1 embeds complementably into $X^{**} \otimes_\varepsilon Y$, that is, a complemented subspace of some $C(K, Y)$ space (see Theorem 2 of [1]). Hence, it is enough to apply the main result of [2] to get our thesis.

Theorem 2. *Let X be a Banach space with X^* isometric to an L^1 space. If Y is a reflexive Banach space, then $X \otimes_\varepsilon Y$ has property* (V) *of Pelczynski.*

Proof. Let T be an unconditionally converging operator on $X \otimes_\varepsilon Y$. The results of [3] imply that T^{**} is unconditionally converging, too. Hence T^{**} restricted to $X^{**} \otimes_\varepsilon Y$ is unconditionally converging; since $X^{**} \otimes_\varepsilon Y$ is complemented in some $C(K, Y)$ space, it inherits property (V) of Pelczynski. Hence T^{**}, and so T, are weakly compact. We are done.

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